

Package: YangHuiMagic (via r-universe)

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Type Package

Title A Generalization of Yang Hui's Magic Squares

Version 1.1

Description The generalized construction methods for magic squares, inspired by the ancient Chinese mathematician Yang Hui's classical work "Xu Gu Zhai Qi Suan Fa". These methods can construct $4n$ -order magic squares and $2(2n+1)$ -order magic squares.

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construct_M *Construct the initial matrix M (satisfying the form of Matrix (8))*

Description

Construct the initial matrix M (satisfying the form of Matrix (8))

Usage

construct_M(n, a11, d1, d2, d12, d21, d22)

Arguments

n	Parameter, final order is 4n
a11	Parameters from the lemma, must satisfy $d12 + d21 = d22$
d1	Parameters from the lemma, must satisfy $d12 + d21 = d22$
d2	Parameters from the lemma, must satisfy $d12 + d21 = d22$
d12	Parameters from the lemma, must satisfy $d12 + d21 = d22$
d21	Parameters from the lemma, must satisfy $d12 + d21 = d22$
d22	Parameters from the lemma, must satisfy $d12 + d21 = d22$

Value

4n x 4n matrix

generate_A11 *Generate the 2n x 2n A11 matrix (arithmetic progression form)*

Description

Generate the 2n x 2n A11 matrix (arithmetic progression form)

Usage

generate_A11(n, a11, d1, d2)

Arguments

n	Parameter, final order is 4n
a11	Upper-left corner starting value
d1	Column direction common difference (horizontal increment)
d2	Row direction common difference (vertical increment)

Value

2n x 2n matrix

generate_symmetric_L *Generate a symmetric L set satisfying the condition (first n numbers and their complements)*

Description

Generate a symmetric L set satisfying the condition (first n numbers and their complements)

Usage

```
generate_symmetric_L(n)
```

Arguments

n Parameter, final order 4n

Value

Integer vector of length 2n

is_magic_square *Verify magic square properties*

Description

Verify magic square properties

Usage

```
is_magic_square(M)
```

Arguments

M Square matrix

Value

TRUE if M satisfies the magic square condition

Examples

```
M=YangConway(m = 2, d_type = "unit", template_set = 1)
is_magic_square(M)
```

odd_magic_square	<i>Construct odd order magic square (Siamese method)</i>
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Description

Construct odd order magic square (Siamese method)

Usage

```
odd_magic_square(k)
```

Arguments

k	Odd order number
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Value

k x k magic square with numbers 1 to k²

Examples

```
odd_magic_square(7)
```

transform_M	<i>Apply row left-right flips and column up-down flips to a matrix</i>
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Description

Apply row left-right flips and column up-down flips to a matrix

Usage

```
transform_M(M, L1, L2)
```

Arguments

M	Initial matrix
L1	Vector of row indices (1-based) to be left-right flipped
L2	Vector of column indices (1-based) to be up-down flipped

Value

Transformed matrix

YangConway	<i>Construct singly even order magic square (Yang-Hui Conway generalization)</i>
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Description

Construct singly even order magic square (Yang-Hui Conway generalization)

Usage

```
YangConway(m, d_type = "square", template_set = 2)
```

Arguments

<code>m</code>	Positive integer, final order $n = 2*(2*m+1)$
<code>d_type</code>	Type of common difference: "unit" ($d=1$) or "square" ($d=(2m+1)^2$)
<code>template_set</code>	Template series: 1~4 corresponding to matrices 4,7,9,10 in the paper

Value

$n \times n$ magic square

Examples

```
# Example 1: Reproduce Yang-Hui 6th order magic square (Yang diagram),
# m=1, d_type="square", template_set=2
cat("==== Yang-Hui 6th order magic square (Yang diagram) =====\n")
yanghui6 <- YangConway(m = 1, d_type = "square", template_set = 2)
print(yanghui6)
cat("Is it a magic square: ", is_magic_square(yanghui6), "\n\n")
# Example 2: Construct 10th order magic square (matrix 8 in the paper),
# m=2, d_type="square", template_set=2
cat("==== 10th order magic square (Yang-Hui method, template 7) =====\n")
yanghui10 <- YangConway(m = 2, d_type = "square", template_set = 2)
print(yanghui10)
cat("Is it a magic square: ", is_magic_square(yanghui10), "\n\n")
# Example 3: Use common difference 1 (LUX method) to construct 10th order magic square, template 4
cat("==== 10th order magic square (LUX method, template 4) =====\n")
lux10 <- YangConway(m = 2, d_type = "unit", template_set = 1)
print(lux10)
cat("Is it a magic square: ", is_magic_square(lux10), "\n\n")
```

YangRamanujan *Construct doubly even order magic square (Yang-Hui · Dürer · Ramanujan inspired)*

Description

Construct doubly even order magic square (Yang-Hui · Dürer · Ramanujan inspired)

Usage

```
YangRamanujan(n, params = "natural", L1 = NULL, L2 = NULL)
```

Arguments

n	Positive integer, order = $4n$
params	Parameter setting. Can be a list containing a11, d1, d2, d12, d21 (d22 is optional, automatically set to d12+d21). Predefined strings: - "natural": natural square parameters (a11=1, d1=1, d2=4n, d12=2n, d21=2n*4n) - "type1" : second row of Table 3 (a11=1, d1=1, d2=2n, d12=(2n)^2, d21=2*(2n)^2) - "type2" : third row of Table 3 (a11=1, d1=4n, d2=1, d12=?, d21=?, d22=?) [values incomplete, for illustration only]
L1	Sets of rows/columns to flip (1-based), default automatically generated symmetric sets
L2	Sets of rows/columns to flip (1-based), default automatically generated symmetric sets

Value

$4n \times 4n$ magic square matrix

Examples

```
# Example 1: Ramanujan's 8th order magic square (matrix 4 in the paper)
# Using natural square parameters, L1 = L2 = {2,3,6,7}
cat("\n==== Ramanujan's 8th order magic square =====\n")
ramanujan8 <- YangRamanujan(n = 2, params = "natural", L1 = c(2, 3, 6, 7), L2 = c(2, 3, 6, 7))
print(ramanujan8)
cat("Is it a magic square: ", is_magic_square(ramanujan8), "\n")
# Example 2: One of Yang-Hui's 4th order magic squares (matrix 2 in the paper)
# For n=1, use natural square, L1 = L2 = {2,3} (rows/columns 1..4 for order 4)
cat("\n==== Yang-Hui 4th order magic square (matrix 2) =====\n")
yanghui4 <- YangRamanujan(n = 1, params = "natural", L1 = c(2, 3), L2 = c(2, 3))
print(yanghui4)
cat("Is it a magic square: ", is_magic_square(yanghui4), "\n")
# Example 3: Dürer's 4th order magic square (matrix 3 in the paper)
# According to Table 1, use specific parameters (n=1) and L1 = L2 = {2,3}
# Parameters from row (22) in Table 1: a11=1, d1=-1, d2=-8, d12=-2, d21=-4, d22=-6
cat("\n==== Dürer's 4th order magic square (matrix 3) =====\n")
```

```
duerer_params <- list(a11 = 1, d1 = 1, d2 = 8, d12 = 2, d21 = 4)
duerer4 <- YangRamanujan(n = 1, params = duerer_params, L1 = c(2, 3), L2 = c(2, 3))
print(duerer4)
cat("Is it a magic square: ", is_magic_square(duerer4), "\n")
# Example 4: Custom 12th order magic square (n=3), using natural square, default symmetric L
cat("\n==== Custom 12th order magic square (natural square, default L) =====\n")
magic12 <- YangRamanujan(n = 3, params = "natural")
# Print only first 6 rows to save space
print(magic12)
cat("Is it a magic square: ", is_magic_square(magic12), "\n")
```

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